

٩٣

مراجعة
فؤاد شمس رابعة
أشغال
م/ذمير عدويت
١٥

أشغال عامة - ٢٠١٣

Foundations

8

Midterm Revision

✱✱ Useful Informations ✱✱

✱ Some of the important functions in calculator Fx-570ES:

1 The function "Table":

• Steps (as an example):

1. Press MODE button.
2. Select TABLE (Choice No. 7).
3. $f(x) = 2X + 2$ (for example)

Hint: To write the equation, as follows:

$$\begin{array}{c} \boxed{2} \quad \boxed{\text{ALPHA}} \quad \boxed{)} \quad + \quad \boxed{2} \\ | \qquad \qquad | \qquad \qquad | \\ 2 \qquad \qquad X \qquad \qquad + \qquad \qquad 2 \end{array}$$

4. Press $\boxed{=}$

5. Start? ← Calculator Screen
1

6. Type 0 0 , then $\boxed{=}$
1

7. End?
5

8. Type 10 10 , then $\boxed{=}$
5

9. 1

10. Type 1 1, then

11.

no. of trials	X	F(x)
1	0	2
2	1	4
3	2	6
4	3	8
⋮	⋮	⋮

This is the table for the equation $f(x) = 2X + 2$ when (x) varies from (0 to 10) with step of (1)

2 The function "Calc":

What if we want to calculate different values of X (not in a pattern form) like fraction values, i.e. 1, 1.5, and 3.

1. Write down the equation $2X + 2$ (as before)

2. Press

3. 10

4. Type 1.5 10, then

5. The result should be = 5

6. Repeat steps 2, 3, and 4 for calculating different values of (X)

3 The function "Solve": (Very..... Very useful function)

If we have an unknown value in one equation, and we want to calculate this unknown value.

Example:

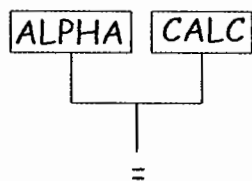
Try to calculate the value of X in the following equation:

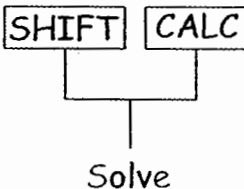
$$\frac{(X^2)^{3/2} + 5X^{0.65}}{\sqrt{(X+1)^2 + 1}} = 3 \longrightarrow \text{Good Luck } \text{😊} !$$

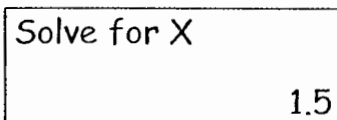
Solution:


1. Write down the equation.

Hint: To write the mark "=", as follows:



2. Press 

3. 

4. Press any number but zero, then 

5. X should be = 1.1765

Question No. (1):-

The foundation of a structure is defined as the part of the structure in direct contact with the ground and which transmits the load of the structure to the ground. Explain the requirements that must be considered during foundation design to realize the above statement.

Answer: -

- ① Stress under footing should not exceed the allowable bearing capacity of soil foundation.
 - ② Rigidity of footing should be achieved considering suitable dimensions and big thickness.
 - ③ Plain concrete footing should be considered if $t_{P.C} \geq 20\text{cm}$.
 - ④ The R.C. footing should be safe [depth] for moments, shear, and punching.
 - ⑤ R.F.T. should be satisfied to the designed moments.
-

Question No. (2):-

Explain the role of tie beams.

Answer: -

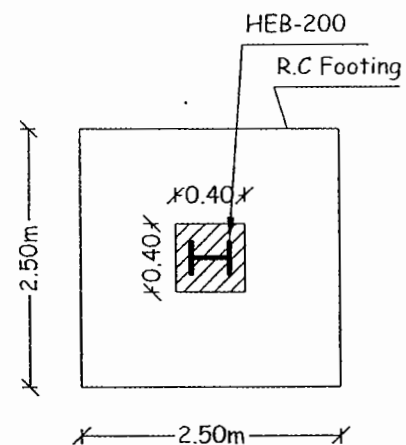
- ① Supporting the walls of basement.
 - ② Connecting the footing to resist the differential settlement.
-

Example No. (1):-

A square R.C. isolated footing is proposed to support a square column of a composite section (as shown in figure). The column carries an axial compression load of 2000 KN. The concrete dimensions of the column cross section are $0.4 \times 0.4\text{m}$. The proposed dimensions of the R.C. footing are $2.5 \times 2.5\text{m}$, and its thickness is 0.5m as estimated from a preliminary design. It is required to check the safety of the proposed footing thickness only for punching shear. If the given footing thickness is unsafe, then estimate the footing thickness that will be safe in punching shear (no further calculations or checks are required).

Given:-

- Column's dimensions = $0.4 \times 0.4\text{m}$
- R.C. footing thickness = 0.50 m
- $f_{cu} = 30\text{ N/mm}^2$



Solution:-Check Punching Shear :-

$$Q_{p_u} = 1.5 * P_w - q_u (X * X)$$

$$= 1.5 * 2000 - 480 * (0.83)^2$$

$$= 2669.33 \text{ KN}$$

$$q_{p_u} = \frac{2669.33 * 10^3}{430 * (830) * 4}$$

$$= 1.87 \text{ N/mm}^2$$

$$q_{p_{cu}} = 0.316 * \left(0.5 + \frac{(0.4)}{(0.4)}\right) \sqrt{\frac{30}{1.5}}$$

$\Rightarrow = 1 \Rightarrow \text{take it} = 0.5$

$$= 1.413 \text{ N/mm}^2$$

$$\therefore q_{p_u} > q_{p_{cu}} \Rightarrow$$

 \therefore UNSAFE \therefore Increase d

take d = 530 mm

$$Q_{p_u} = 1.5 * 2000 - 480 * (0.93)^2$$

$$= 2584.85 \text{ KN}$$

$$q_{p_u} = \frac{2584.85 * 10^3}{530 * (930) * 4}$$

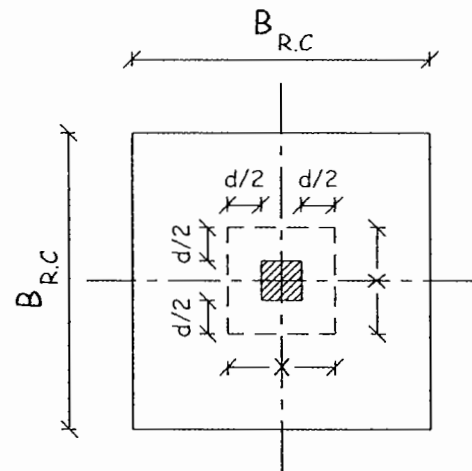
$$= 1.311 \text{ N/mm}^2$$

$$\therefore q_{p_u} < q_{p_{cu}} \Rightarrow$$

 \therefore SAFE

$$d_{\text{final}} = 530 \text{ mm}$$

$$t_{\text{final}} = 530 + 70 (\text{cover}) = 600 \text{ mm}$$



$$X = 0.4 + 0.43 = 0.83 \text{ m}$$

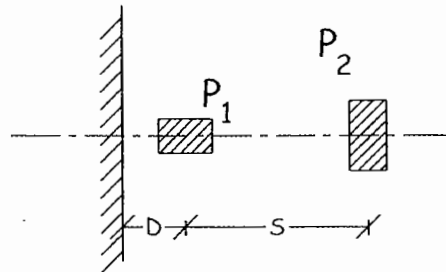
$$q_u = \frac{1.5 * 2000}{2.5 * 2.5}$$

$$= 480 \text{ KN/m}^2$$

Choosing a foundation system near the property line: (As in lecture)

To choose a suitable foundation system for the property line, we shall try the solutions in the following two cases:-

(1) Case of the outer column has a distance "D":-



اختصاراً لخطوات المسألة وتوفيراً لوقت الامتحان يتم اتباع الحلول الآتية بالترتيب لاختيار القاعدة المناسبة.

يتم البدء بالقاعدة المنفصلة وفي حالة فشلها نحدد إذا كانت المسافة بين العمودين أصغر أو يساوي أو أكبر من 5.0 m لتحديد أي نوع من القواعد سنلجأ لها كالآتي :-

1 - Isolated. $\frac{1}{2} \sqrt{\frac{P_{col.}}{q_{all.}}} \not> D$

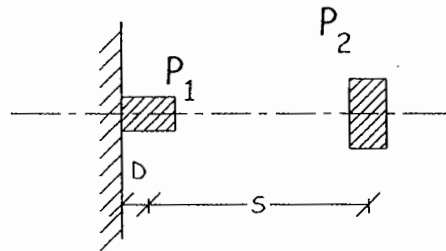
2- $P_1 < P_2$

$S \leq 5.0 \text{ m}$
Combined Rectangular.

في حالة فشل
Strap Beam I

$S > 5.0 \text{ m}$
Strap Beam

(2) Case of the outer column is adjacent to the property line:-



1- $P_1 < P_2$

$S \leq 5.0 \text{ m}$

Combined Rectangular.

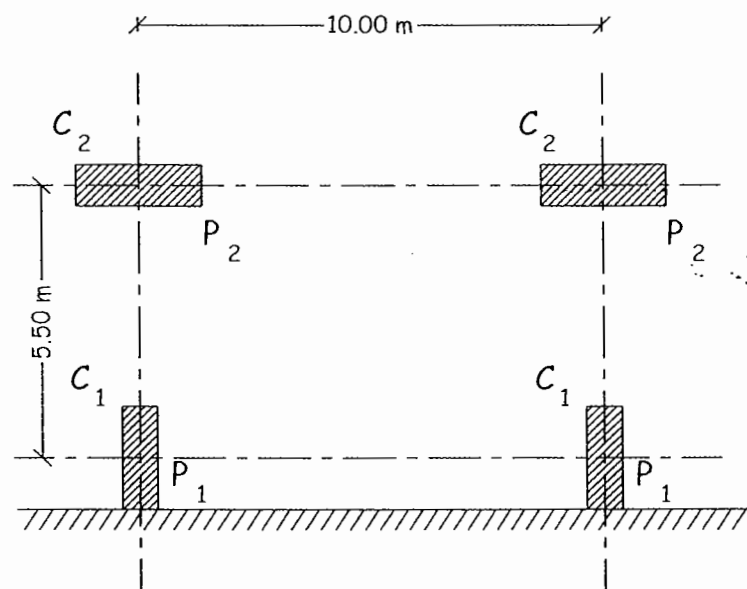
$S > 5.0 \text{ m}$

Strap Beam

في حالة فشل
Strap Beam II

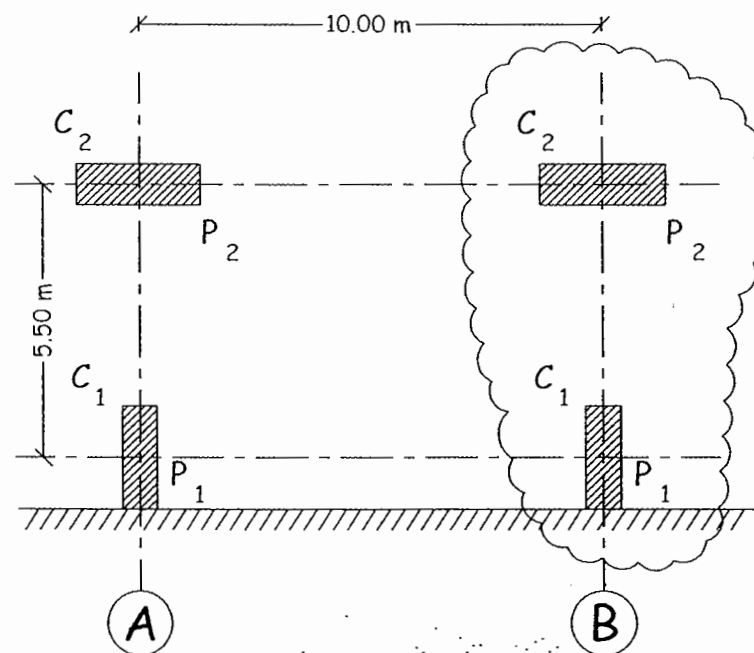
Example No. (2):-

It is required to design suitable and economic foundation system (s) to support the given columns in the part plan shown in the figure. Also, draw sketches illustrating the details of the foundations for both concrete dimensions and reinforcement.

**Given:-**

- $t_{P.C} = 40 \text{ cm}$
- $q_{all.} = 150 \text{ Kpa}$
- $f_{cu} = 30 \text{ N/mm}^2$
- $f_y = 360 \text{ N/mm}^2$
- $C_1 (0.5 * 1.5)\text{m} , P_1 = 4500 \text{ KN}$
- $C_2 (0.6 * 1.8)\text{m} , P_2 = 6500 \text{ KN}$

Solution:-



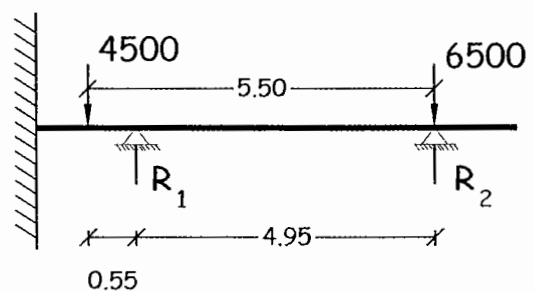
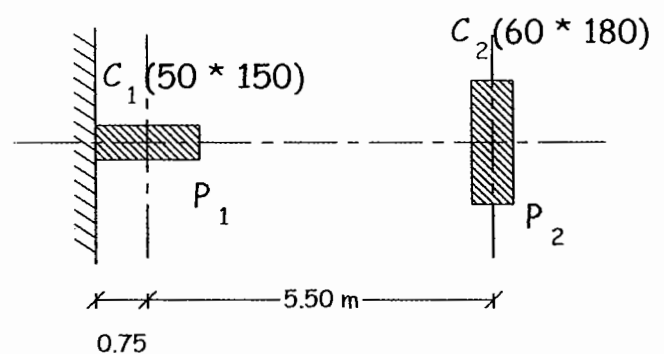
For the two columns C_1, C_2 (Axis A or B), we shall design a strap beam footing as a foundation system.

$$\text{assume } e = (0.1 \rightarrow 0.2) * 5.50$$

$$e = 0.55 \text{ m}$$

$$\therefore R_1 = \frac{4500 * 5.50}{4.95} = 5000 \text{ KN}$$

$$\begin{aligned} \therefore R_2 &= [4500 + 6500] - 5000 \\ &= 6000 \text{ KN} \end{aligned}$$



① Calculate the footing area :-

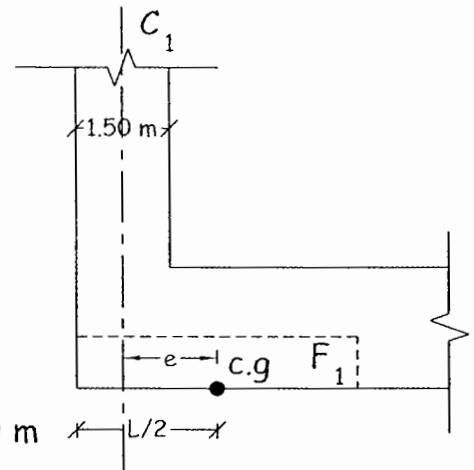
For $[F_1]$

$$\therefore t_{p,c} = 40 \text{ cm} > 20 \text{ cm}$$

$$\therefore A_{p,c} = \frac{R_1}{q_{all}} = \frac{5000}{150} = 33.33 \text{ m}^2$$

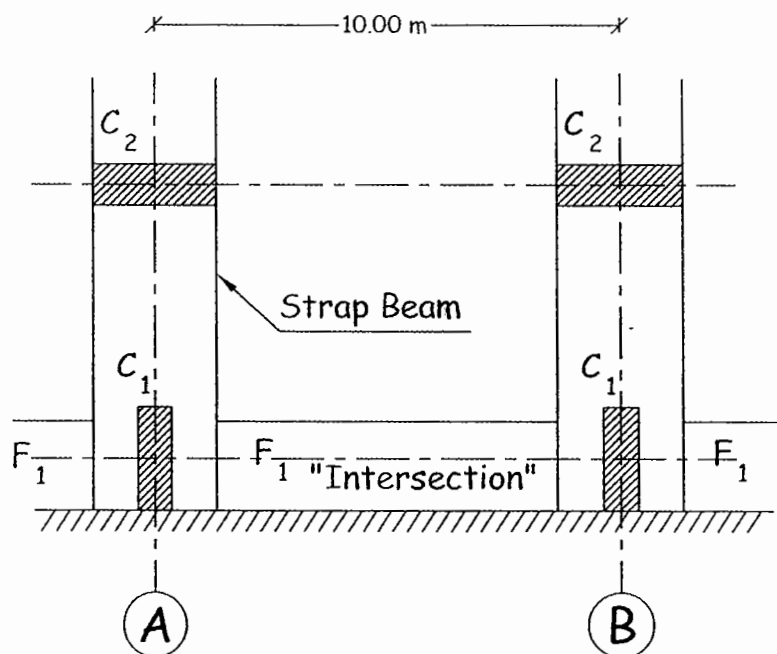
$$L_{p,c} = 2 \left[e + \frac{C}{2} \right] = 2 \left[0.55 + \frac{1.5}{2} \right] = 2.60 \text{ m}$$

$$\therefore B_{p,c} = \frac{A_{p,c}}{L_{p,c}} = \frac{33.33}{2.60} = \underline{\underline{12.82 \text{ m}}}$$



Since the distance between Axis A & B = 10.00 m

سيحدث تداخل بين القاعدتين F_1 على محور A & B \therefore

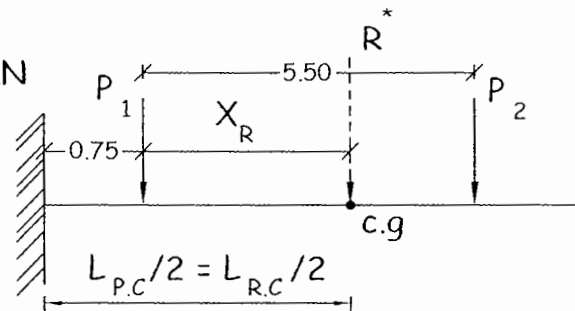


\therefore We can't use strap beam

\therefore Use combined footing $\Rightarrow \therefore P_1 < P_2 \Rightarrow \therefore$ Use rectangular combined

$$R^* = P_1 + P_2 = 4500 + 6500 = 11000 \text{ KN}$$

$$X_R = \frac{6500 * 5.50}{11000} = 3.25 \text{ m}$$



① Calculate the footing area :-

$$\frac{L_{p.c}}{2} = X_R + D = 3.25 + 0.75 = 4.00 \text{ m}$$

$$L_{p.c} = 2 * 4.00 = 8.00 \text{ m}$$

$$L_{p.c} = L_{r.c} = 8.00 \text{ m}$$

$$\therefore t_{p.c} = 40 \text{ cm} > 20 \text{ cm}$$

$$\therefore A_{p.c} = \frac{R^*}{q_{all.}} = \frac{11000}{150} = 73.33 \text{ m}^2 = B_{p.c} * 8.00$$

$$\therefore B_{p.c} = \frac{A_{p.c}}{L_{p.c}} = \frac{73.33}{8.00} = 9.20 \text{ m} < 10.00 \text{ m} \Rightarrow \therefore \text{O.K.}$$

$$B_{r.c} = 9.20 - 2 * 0.40 = 8.40 \text{ m}$$

② Design in long direction:-

$$P_{1u} = 1.5 * 4500 = 6750 \text{ KN}$$

$$P_{2u} = 1.5 * 6500 = 9750 \text{ KN}$$

$$R_u^* = 1.5 * 11000 = 16500 \text{ KN}$$

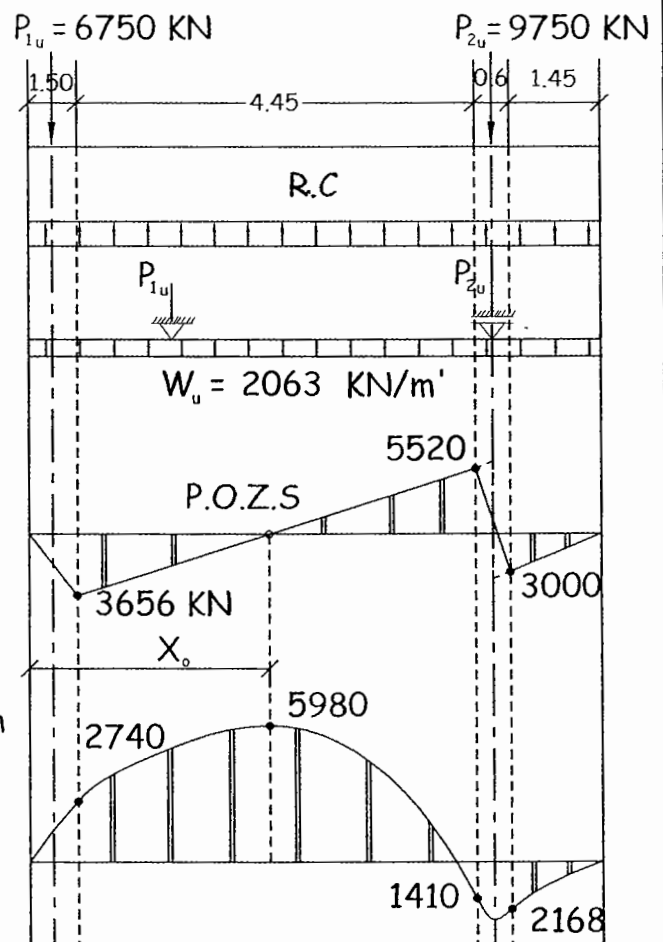
$$W_u = \frac{16500}{8.00} = 2063 \text{ KN/m'}$$

$$q_u = \frac{16500}{8.00 * 8.40} = 246 \text{ KN/m}^2$$

* get the point of zero shear:-

$$6750 = 2063 * X_o \Rightarrow X_o = 3.27 \text{ m}$$

$$\begin{aligned} M_{max.} &= 2063 * \frac{3.27^2}{2} \\ &\quad - 6750 [3.27 - 0.75] \\ &= -5980 \text{ KN.m} \end{aligned}$$



$$\therefore d = 5 \sqrt{\frac{M_{\max.} * 10^6}{f_{cu} * (B_{R.C.})_{(mm)}}} = 5 \sqrt{\frac{5980 * 10^6}{30 * 8400}} = 793.4 \text{ mm}$$

$$\text{take } d = 830 \text{ mm}$$

③ Check Shear :-

$$Q_{\max.} = 5520 \text{ KN}$$

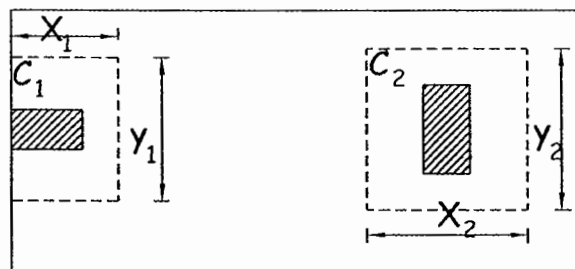
$$Q_{su} = Q_{\max.} - W * \frac{d}{2} = 5520 - 2063 * \frac{0.83}{2} = 4663.86 \text{ KN}$$

$$q_{su} = \frac{Q_{su} * 10^3}{d * B} = \frac{4663.86 * 10^3}{830 * 8400} = 0.669 \text{ N/mm}^2$$

$$q_{scu} = 0.16 \sqrt{\frac{F_{cu}}{\gamma_c}} = 0.16 \sqrt{\frac{30}{1.5}} = 0.72 \text{ N/mm}^2$$

$$\therefore q_{su} < q_{scu} \Rightarrow \therefore \text{SAFE}$$

④ Check Punching Shear :-



For C_1

$$X_1 = 1.5 + \frac{0.83}{2} = 1.915 \text{ m}$$

$$Y_1 = 0.5 + 0.83 = 1.33 \text{ m}$$

$$Q_{p_1} = 6750 - 246 * (1.915 * 1.33) \\ = 6123.45 \text{ KN}$$

For C_2

For C₁

$$q_{p1} = \frac{6123.45 * 10^3}{830 * [2 * 1915 + 1330]} = 1.43 \text{ N/mm}^2$$

$$q_{p_{cu1}} = 0.316 \left(0.5 + \frac{0.5}{1.5} \right) \sqrt{\frac{30}{1.5}} \\ = 1.18 \text{ N/mm}^2$$

$$\therefore q_{p1} > q_{p_{cu1}} \Rightarrow \therefore \text{UNSAFE}$$

$$\text{take } d = 930 \text{ mm}$$

$$X_1 = 1.5 + \frac{0.93}{2} = 1.965 \text{ m}$$

$$Y_1 = 0.5 + 0.93 = 1.43 \text{ m}$$

$$Q_{p1} = 6750 - 246 * (1.965 * 1.43) \\ = 6058.8 \text{ KN}$$

$$q_{p1} = \frac{6058.8 * 10^3}{930 * [2 * 1965 + 1430]} = 1.22 \text{ N/mm}^2$$

$$\therefore q_{p1} > q_{p_{cu1}} \Rightarrow \therefore \text{UNSAFE}$$

$$\text{take } d = 980 \text{ mm}$$

$$X_1 = 1.5 + \frac{0.98}{2} = 1.99 \text{ m}$$

$$Y_1 = 0.5 + 0.98 = 1.48 \text{ m}$$

$$Q_{p1} = 6750 - 246 * (1.99 * 1.48) \\ = 5972 \text{ KN}$$

$$q_{p1} = \frac{5972 * 10^3}{980 * [2 * 1990 + 1480]} = 1.12 \text{ N/mm}^2$$

$$\therefore q_{p1} < q_{p_{cu1}} \Rightarrow \therefore \text{SAFE}$$

For C₂

$$X_2 = 1.8 + 0.98 = 2.78 \text{ m}$$

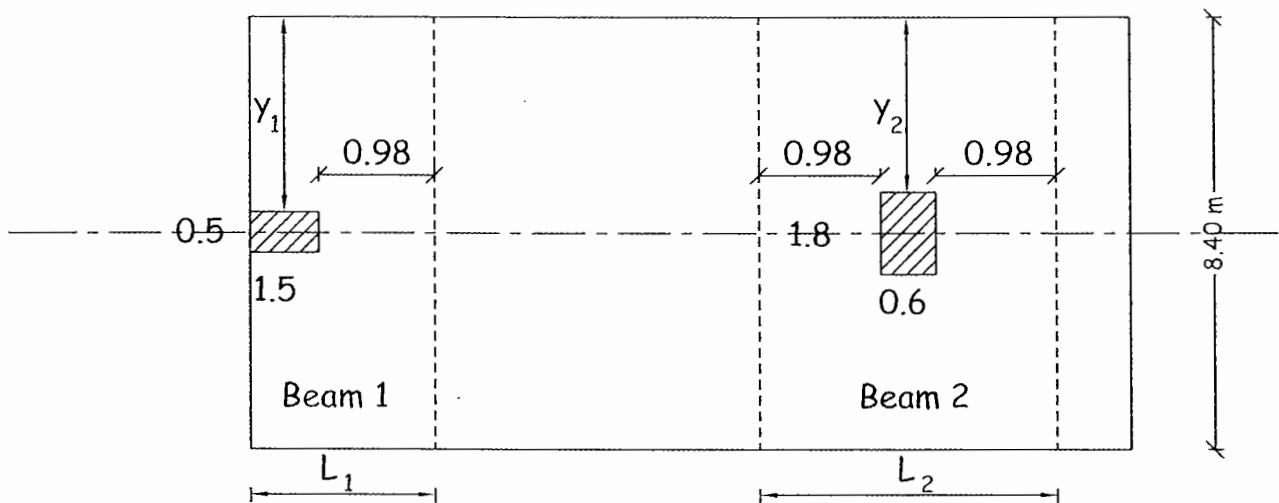
$$Y_2 = 0.6 + 0.98 = 1.58 \text{ m}$$

$$Q_{p2} = 9750 - 246 * (2.78 * 1.58) \\ = 8670 \text{ KN}$$

$$q_{p2} = \frac{8670 * 10^3}{980 * [2780 + 1580] * 2} = 1.014 \text{ N/mm}^2$$

$$q_{p_{cu2}} = 0.316 * \left(0.5 + \frac{0.6}{1.8} \right) \sqrt{\frac{30}{1.5}} \\ = 1.18 \text{ N/mm}^2$$

$$\therefore q_{p2} < q_{p_{cu2}} \Rightarrow \therefore \text{SAFE}$$

⑤ Design in short direction:-For Beam 1

$$L_1 = 1.5 + 0.98 = 2.48 \text{ m}$$

$$\therefore q_{u1} = \frac{6750}{8.40 \times 2.48} = 334.8 \text{ KN/m}^2$$

$$\therefore y_1 = \frac{8.40 - 0.50}{2} = 3.95 \text{ m}$$

$$\begin{aligned} \therefore M_1 &= 334.8 \times \frac{3.95^2}{2} \times 1\text{m} \\ &= 2611.9 \text{ KN.m/m} \end{aligned}$$

For Beam 2

$$L_2 = 0.6 + 2 \times 0.98 = 2.56 \text{ m}$$

$$\therefore q_{u2} = \frac{9750}{8.40 \times 2.56} = 453.4 \text{ KN/m}^2$$

$$\therefore y_2 = \frac{8.40 - 1.80}{2} = 3.30 \text{ m}$$

$$\begin{aligned} \therefore M_2 &= 453.4 \times \frac{3.30^2}{2} \times 1\text{m} \\ &= 2468.76 \text{ KN.m/m} \end{aligned}$$

$$M_{\text{bigger}} = M_1 = 2611.9 \text{ KN.m/m}$$

$$\therefore d = 980 = C_1 \sqrt{\frac{2611.9 \times 10^6}{30 \times 1000}} \Rightarrow C_1 = 3.32 > 2.8 \therefore \text{SAFE}$$

⑥ Final Thickness :-

$$d_{\text{final}} = 980 \text{ mm}$$

$$t_{\text{final}} = 980 + 70 (\text{cover}) = 1050 \text{ mm}$$

⑦ R.F.T:-

$$A_{s_{min}} = \left\{ \begin{array}{l} 1.5 * d_{mm} = 1.5 * 980 = 1470 \text{ mm}^2/\text{m}' \\ 5 \Phi 12/\text{m}' = 565 \text{ mm}^2/\text{m}' \end{array} \right\} \boxed{8 \Phi 16/\text{m}'}$$

In Long direction:-

$$A_{s_{Top}} = \frac{M_{u_{top}} * 10^6 / B}{F_y * J * d} = \frac{5980 * 10^6 / 8.40}{360 * 0.826 * 980} = 2442.9 \text{ mm}^2/\text{m}'$$

$$\boxed{7 \Phi 22/\text{m}'}$$

$$A_{s_{Bottom}} = \frac{M_{u_{bot}} * 10^6 / B}{F_y * J * d} = \frac{2168 * 10^6 / 8.40}{360 * 0.826 * 980} = 890 \text{ mm}^2/\text{m}' < A_{s_{min}}$$

$$\text{use } A_{s_{min}} \quad \boxed{8 \Phi 16/\text{m}'}$$

In Short direction:-

$$A_{s_1} = \frac{M_{u_1} * 10^6}{F_y * J * d} = \frac{2611.9 * 10^6}{360 * 0.77 * 980} = 9615 \text{ mm}^2/\text{m}'$$

$$\boxed{14 \Phi 32/\text{m}'}$$

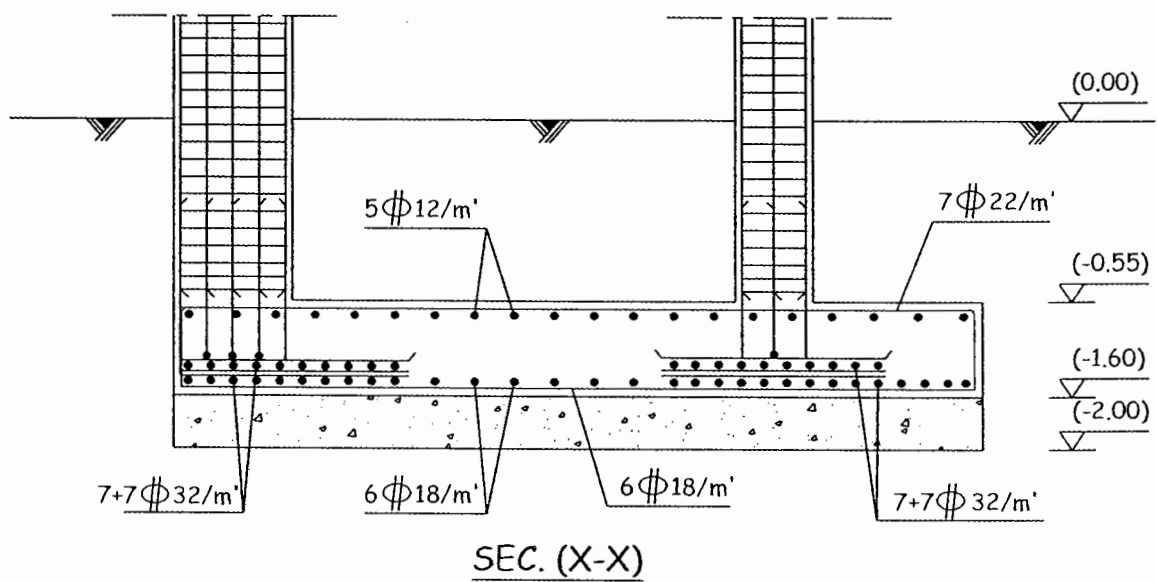
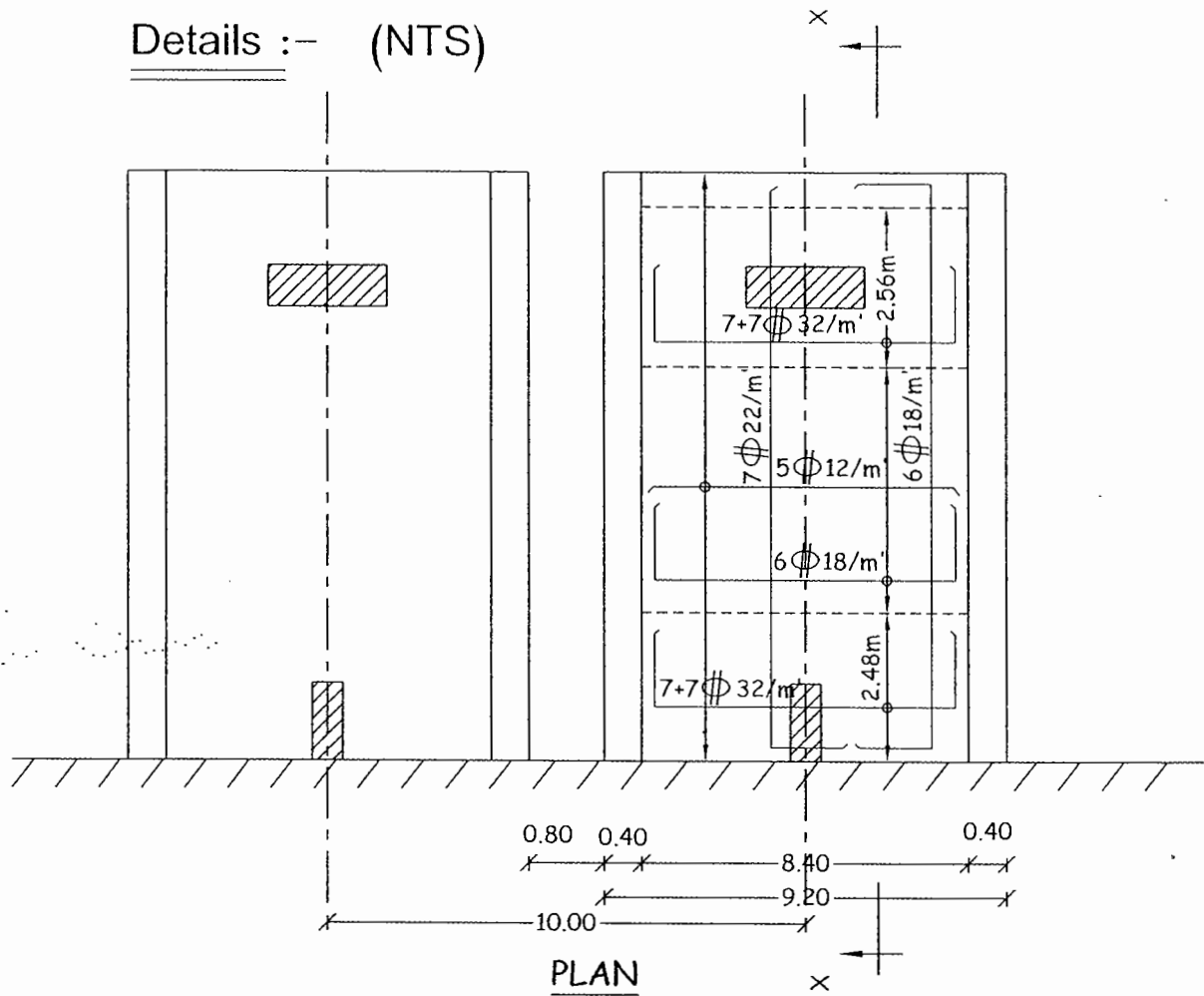
on two rows

$$A_{s_2} = \frac{M_{u_2} * 10^6}{F_y * J * d} = \frac{2468.8 * 10^6}{360 * 0.77 * 980} = 9088 \text{ mm}^2/\text{m}'$$

$$\boxed{14 \Phi 32/\text{m}'}$$

on two rows

Details :- (NTS)

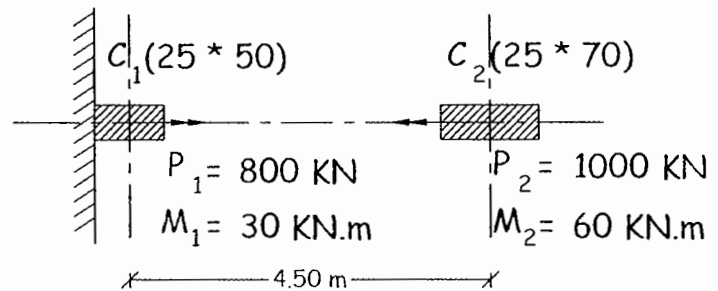


Example No. (3):-

For the shown two columns beside the property line of a building, it is required to design a suitable foundation system to support the two columns under the given loads (normal loads and moments on the columns are considered), full detail (scale 1:50) in plan and elevation are required.

Given:-

- $t_{P.C} = 40 \text{ cm}$
- $q_{all} = 150 \text{ Kpa}$
- $f_{cu} = 30 \text{ N/mm}^2$
- $f_y = 360 \text{ N/mm}^2$

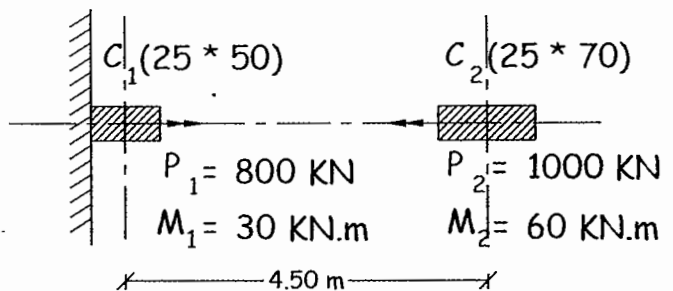
**Solution:-**

C_1 ملاصق لحد الجار

Isolated footing حل لا يصلح

$$\therefore S = 4.50 \text{ m}$$

\therefore Try Combined Rect.

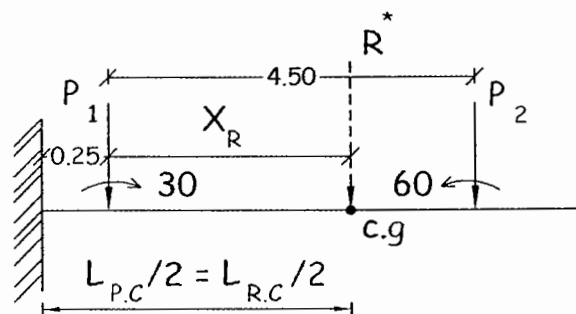


$$R^* = P_1 + P_2 = 800 + 1000 = 1800 \text{ kN}$$

$$\sum M_{C_1} = \text{Zero}$$

$$\therefore 1000 * 4.50 + 30 - 60 = X_R * 1800$$

$$X_R = 2.48 \text{ m}$$



① Calculate the footing area :-

$$\frac{L_{P.C}}{2} = X_R + D = 2.48 + 0.25 = 2.73 \text{ m} \approx 2.75 \text{ m}$$

$$L_{P.C} = 2 * 2.75 = 5.50 \text{ m}$$

$$L_{P.C} = L_{R.C} = 5.50 \text{ m}$$

$$\therefore t_{P.C} = 40 \text{ cm} > 20 \text{ cm}$$

$$\therefore A_{P.C} = \frac{R^*}{q_{all.}} = \frac{1800}{150} = 12 \text{ m}^2 = B_{P.C} * 5.50$$

$$\therefore B_{P.C} = \frac{A_{P.C}}{L_{P.C}} = \frac{12}{5.50} = 2.18 \text{ m} \approx 2.20 \text{ m}$$

$$B_{R.C} = 2.20 - 2 * 0.40 = 1.40 \text{ m}$$

② Design in long direction:-

$$P_{1u} = 1.5 * 800 = 1200 \text{ KN}$$

$$P_{2u} = 1.5 * 1000 = 1500 \text{ KN}$$

$$R_u^* = 1.5 * 1800 = 2700 \text{ KN}$$

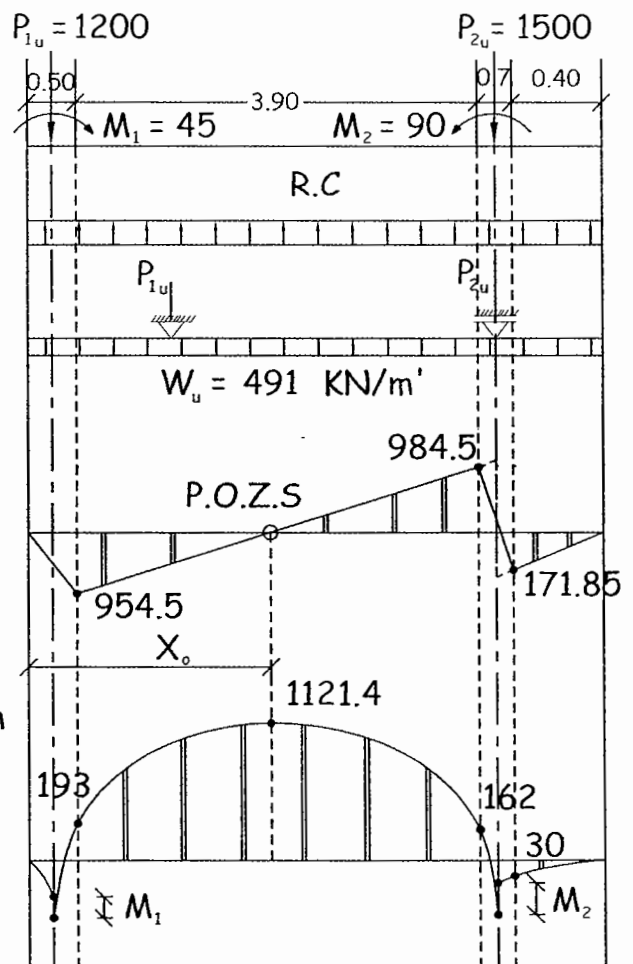
$$W_u = \frac{2700}{5.50} = 491 \text{ KN/m'}$$

$$q_u = \frac{2700}{5.50 * 1.40} = 350.65 \text{ KN/m}^2$$

* get the point of zero shear:-

$$1200 = 491 * X_o \Rightarrow X_o = 2.44 \text{ m}$$

$$\begin{aligned} M_{max.} &= 491 * \frac{2.44^2}{2} + (45) \\ &\quad - 1200 [2.44 - 0.25] \\ &= -1121.4 \text{ KN.m} \end{aligned}$$



$$\therefore d = 5 \sqrt{\frac{M_{\max.} \cdot 10^6}{f_{cu} \cdot (B_{R.C.})_{(mm)}}} = 5 \sqrt{\frac{1121.4 \cdot 10^6}{30 \cdot 1400}} = 817 \text{ mm}$$

$$\boxed{\text{take } d = 830 \text{ mm}}$$

③ Check Shear :-

$$Q_{\max.} = 984.5 \text{ kN}$$

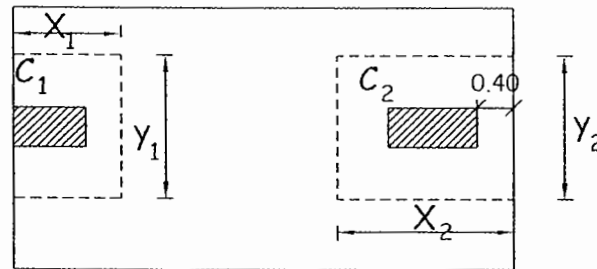
$$Q_{su} = Q_{\max.} - W \cdot \frac{d}{2} = 984.5 - 491 \cdot \frac{0.83}{2} = 780.7 \text{ kN}$$

$$q_{su} = \frac{Q_{su} \cdot 10^3}{d \cdot B} = \frac{780.7 \cdot 10^3}{830 \cdot 1400} = 0.67 \text{ N/mm}^2$$

$$q_{scu} = 0.16 \sqrt{\frac{F_{cu}}{\gamma_c}} = 0.16 \sqrt{\frac{30}{1.5}} = 0.72 \text{ N/mm}^2$$

$$\therefore q_{su} < q_{scu} \Rightarrow \therefore \text{SAFE}$$

④ Check Punching Shear :-

For C₁

$$X_1 = 0.5 + \frac{0.83}{2} = 0.915 \text{ m}$$

$$Y_1 = 0.25 + 0.83 = 1.08 \text{ m}$$

$$Q_{p_1} = 1200 - 350.65 * (1.08 * 0.915) \\ = 853.5 \text{ kN}$$

$$q_{p_1} = \frac{853.5 * 10^3}{830 * [2 * 915 + 1080]} = 0.35 \text{ N/mm}^2$$

$$q_{p_{cu_1}} = 0.316 * \left(0.5 + \frac{0.25}{0.5}\right) \sqrt{\frac{30}{1.5}} \\ = 1.413 \text{ N/mm}^2$$

$$\therefore q_{p_1} < q_{p_{cu_1}} \Rightarrow \therefore \text{SAFE}$$

For C₂

$$X_2 = 0.7 + \frac{0.83}{2} + 0.40 = 1.515 \text{ m}$$

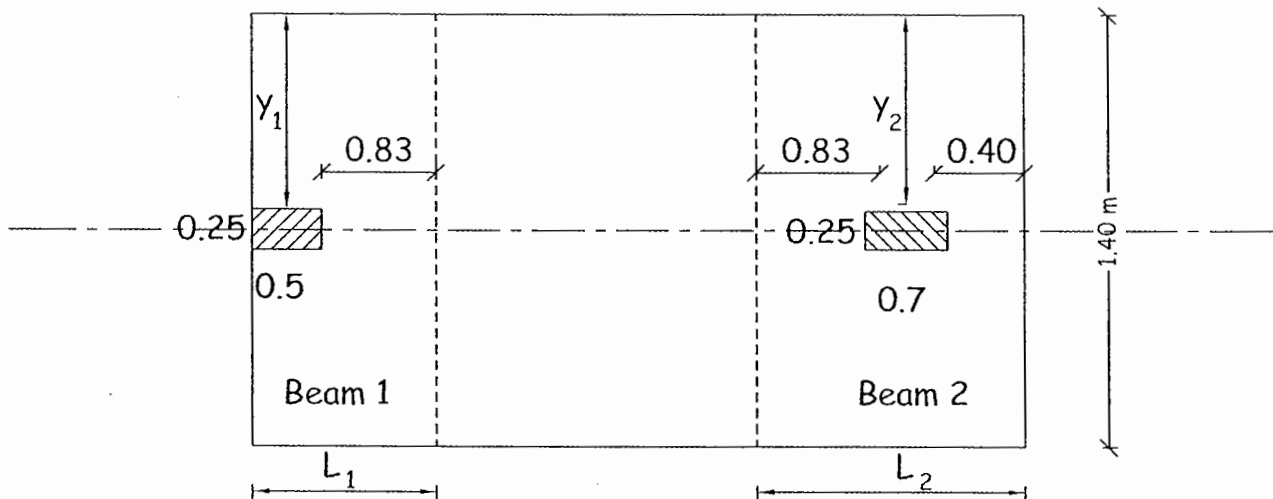
$$Y_2 = 0.25 + 0.83 = 1.08 \text{ m}$$

$$Q_{p_2} = 1500 - 350.65 * (1.515 * 1.08) \\ = 926.27 \text{ kN}$$

$$q_{p_2} = \frac{926.27 * 10^3}{830 * [2 * 1515 + 1080]} = 0.27 \text{ N/mm}^2$$

$$q_{p_{cu_2}} = 0.316 * \left(0.5 + \frac{0.25}{0.70}\right) \sqrt{\frac{30}{1.5}} \\ = 1.21 \text{ N/mm}^2$$

$$\therefore q_{p_2} < q_{p_{cu_2}} \Rightarrow \therefore \text{SAFE}$$

⑤ Design in short direction:-For Beam 1

$$L_1 = 0.5 + 0.83 = 1.33 \text{ m}$$

$$\therefore q_{u_1} = \frac{1200}{1.40 \times 1.33} = 644.5 \text{ KN/m}^2$$

$$\therefore y_1 = \frac{1.40 - 0.25}{2} = 0.575 \text{ m}$$

$$\begin{aligned} \therefore M_1 &= 644.5 \times \frac{0.575^2}{2} \times 1 \text{ m} \\ &= 106.5 \text{ KN.m/m'} \end{aligned}$$

For Beam 2

$$L_2 = 0.7 + 0.83 + 0.40 = 1.93 \text{ m}$$

$$\therefore q_{u_2} = \frac{1500}{1.40 \times 1.93} = 555 \text{ KN/m}^2$$

$$\therefore y_2 = \frac{1.40 - 0.25}{2} = 0.575 \text{ m}$$

$$\begin{aligned} \therefore M_2 &= 555 \times \frac{0.575^2}{2} \times 1 \text{ m} \\ &= 91.75 \text{ KN.m/m'} \end{aligned}$$

$$M_{\text{bigger}} = M_1 = 106.5 \text{ KN.m/m'}$$

$$\therefore d = 830 = C_1 \sqrt{\frac{106.5 \times 10^6}{30 \times 1000}} \Rightarrow C_1 = 13.9 > 2.8 \therefore \text{SAFE}$$

⑥ Final Thickness :-

$$d_{\text{final}} = 830 \text{ mm}$$

$$t_{\text{final}} = 830 + 70 (\text{cover}) = 900 \text{ mm}$$

⑦ R.F.T:-

$$A_{s_{min.}} = \left\{ \begin{array}{l} 1.5 * d_{mm} = 1.5 * 830 = 1245 \text{ mm}^2/\text{m}' \\ 5 \Phi 12/\text{m}' = 565 \text{ mm}^2/\text{m}' \end{array} \right\} \boxed{7 \Phi 16/\text{m}'}$$

In Long direction:-

$$A_{s_{Top}} = \frac{M_{u_{top}} * 10^6 / B}{F_y * J * d} = \frac{1121.4 * 10^6 / 1.40}{360 * 0.826 * 830} = 3260 \text{ mm}^2/\text{m}'$$

$$\boxed{9 \Phi 22/\text{m}'}$$

$$A_{s_{Bottom}} = \frac{M_{u_{bot.}} * 10^6 / B}{F_y * J * d} = \frac{30 * 10^6 / 1.40}{360 * 0.826 * 830} = 86 \text{ mm}^2/\text{m}' < A_{s_{min.}}$$

$$\text{use } A_{s_{min.}} \quad \boxed{7 \Phi 16/\text{m}'}$$

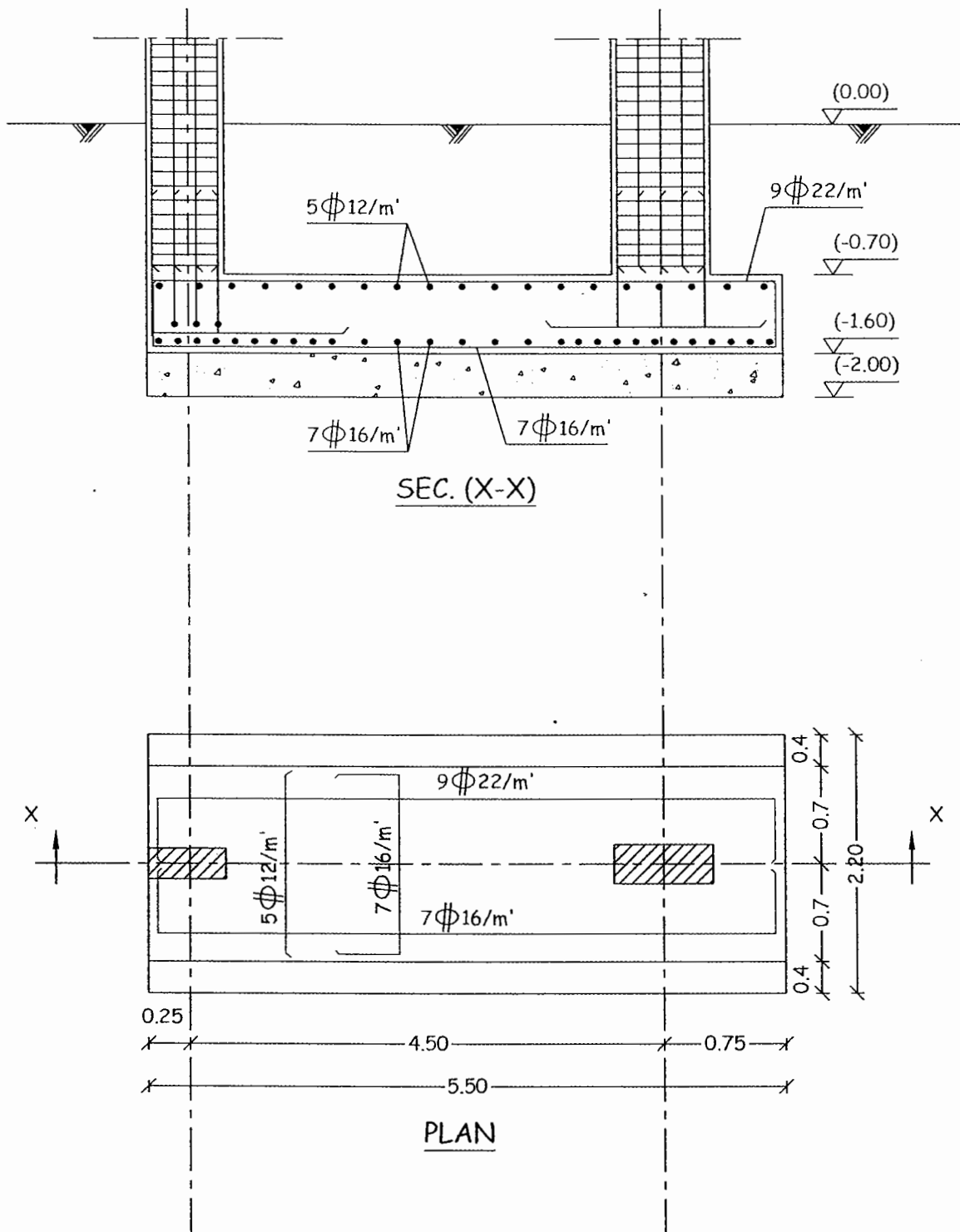
In Short direction:-

$$A_{s_1} = \frac{M_{u_1} * 10^6}{F_y * J * d} = \frac{106.5 * 10^6}{360 * 0.826 * 830} = 431 \text{ mm}^2/\text{m}' < A_{s_{min.}}$$

$$A_{s_2} = \frac{M_{u_2} * 10^6}{F_y * J * d} = \frac{94.2 * 10^6}{360 * 0.826 * 830} = 381 \text{ mm}^2/\text{m}' < A_{s_{min.}}$$

$$\text{use } A_{s_{min.}} \quad \boxed{7 \Phi 16/\text{m}'}$$

⑧ Details :-

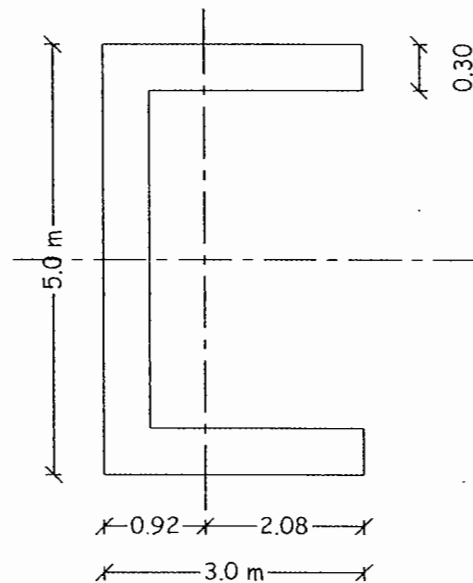
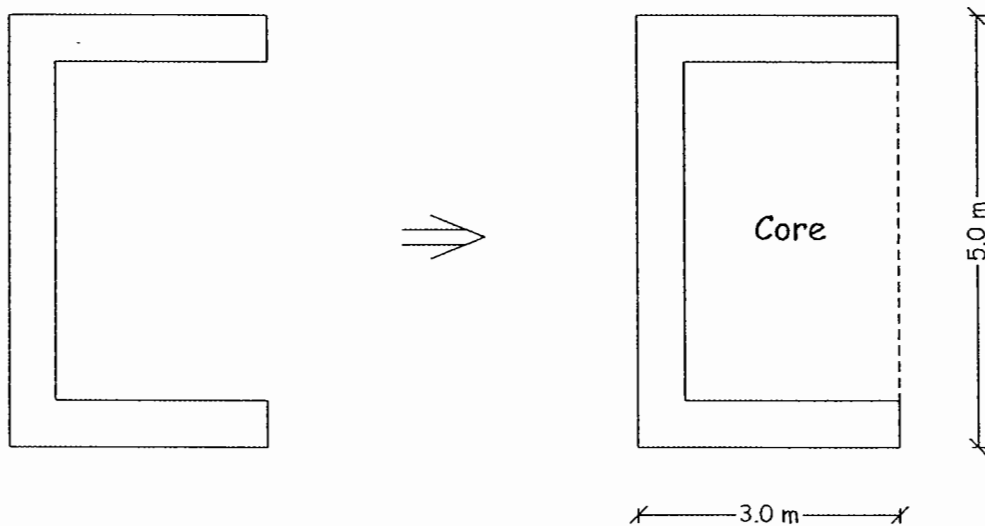


Example No. (4):-

For the shown reinforced concrete core, design a suitable foundation assuming rigid footing. The core is carrying net working load of 1000 ton, the net bearing capacity of supporting soil is 20 t/m^2 .

Given:-

- $f_{cu} = 30 \text{ N/mm}^2$
- $f_y = 400 \text{ N/mm}^2$

**Solution:-**

① Calculate the footing area :-

$$\text{assume } t_{P.C} = 10 \text{ cm} < 20 \text{ cm}$$

$$\therefore A_{R.C} = \frac{10000}{200} = 50 \text{ m}^2 = B_{R.C} * L_{R.C} \text{ ----- } \textcircled{1}$$

$$L_{R.C} - B_{R.C} = b - a$$

$$L_{R.C} - B_{R.C} = 5 - 3 = 2 \text{ m} \text{ ----- } \textcircled{2}$$

Solving ① & ② :-

$$50 = B_{R.C} * (2 + B_{R.C}) \Rightarrow B_{R.C} = 6.14 \approx 6.15 \text{ m}$$

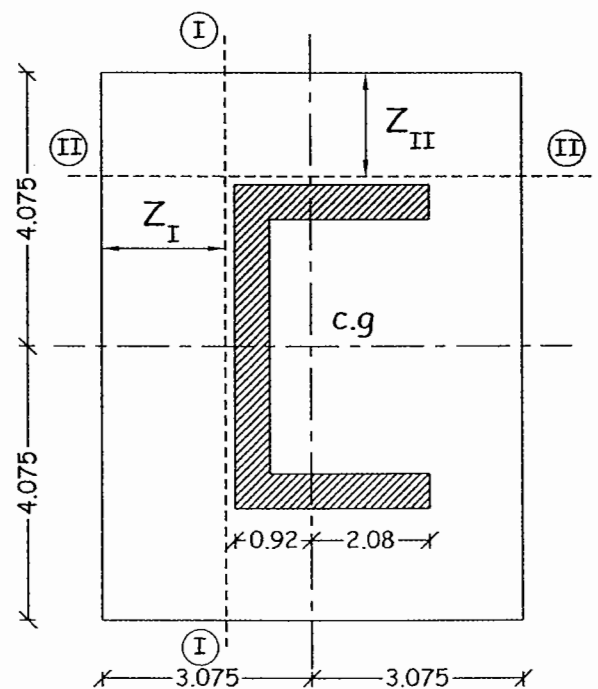
$$L_{R.C} = 2 + B_{R.C} = 2 + 6.15 = 8.15 \text{ m}$$

$$L_{P.C} = 8.15 + 2 * 0.10 = 8.35 \text{ m}$$

$$B_{P.C} = 6.15 + 2 * 0.10 = 6.35 \text{ m}$$

② Ultimate loads :-

$$q_u = \frac{1.5 * 10000}{8.15 * 6.15} = 299.3 \text{ KN/m}^2$$



③ Critical section for moment (M) :-

** For sec (I-I)

$$Z_I = \frac{1}{2} (8.15 - 5) = 1.575 \text{ m}$$

$$\therefore M_{u_I} = 299.3 * \frac{1.575^2}{2} * 1 \text{ m}$$

$$= 371.22 \text{ KN.m/m'}$$

** For sec (II-II)

$$Z_{II} = 3.075 - 0.92 = 2.155 \text{ m}$$

$$\therefore M_{u_{II}} = 299.3 * \frac{2.155^2}{2} * 1 \text{ m}$$

$$= 695 \text{ KN.m/m'}$$

$$M_{\text{bigger}} = M_{u_{II}} = 695 \text{ KN.m/m'}$$

$$d_{II} = 5 \sqrt{\frac{695 * 10^6}{30 * 1000}} = 761 \text{ mm} \approx 780 \text{ mm}$$

④ Check Shear :-

$$\ell = Z_{II} - \frac{d}{2} = 2.155 - \frac{0.78}{2} = 1.765 \text{ m}$$

$$Q_{su} = q_u * \ell * 1 \text{ m} = 299.3 * 1.765 * 1 \text{ m} = 528.3 \text{ KN/m'}$$

$$q_{su} = \frac{Q_{su} * 10^3}{d * B} = \frac{528.3 * 10^3}{780 * 1000} = 0.677 \text{ N/mm}^2$$

$$q_{scu} = 0.16 \sqrt{\frac{F_{cu}}{\gamma_c}} = 0.16 \sqrt{\frac{30}{1.5}} = 0.715 \text{ N/mm}^2$$

$$\therefore q_{su} < q_{scu} \Rightarrow \therefore \text{SAFE}$$

⑤ Check Punching Shear :-

The given column works as a core (acts as a wall), therefore no punching shear check shall be calculated.

⑥ Final Thickness :-

$$d_{\text{final}} = 780 \text{ mm}$$

$$t_{\text{final}} = 780 + 70 (\text{cover}) = 850 \text{ mm}$$

⑦ R.F.T :-

$$A_{s_{\text{min}}} = \left\{ \begin{array}{l} 1.5 * d_{\text{mm}} = 1.5 * 780 = 1170 \text{ mm}^2/\text{m}' \\ 5 \phi 12/\text{m}' = 565 \text{ mm}^2/\text{m}' \end{array} \right\} \quad \boxed{6 \phi 16/\text{m}'}$$

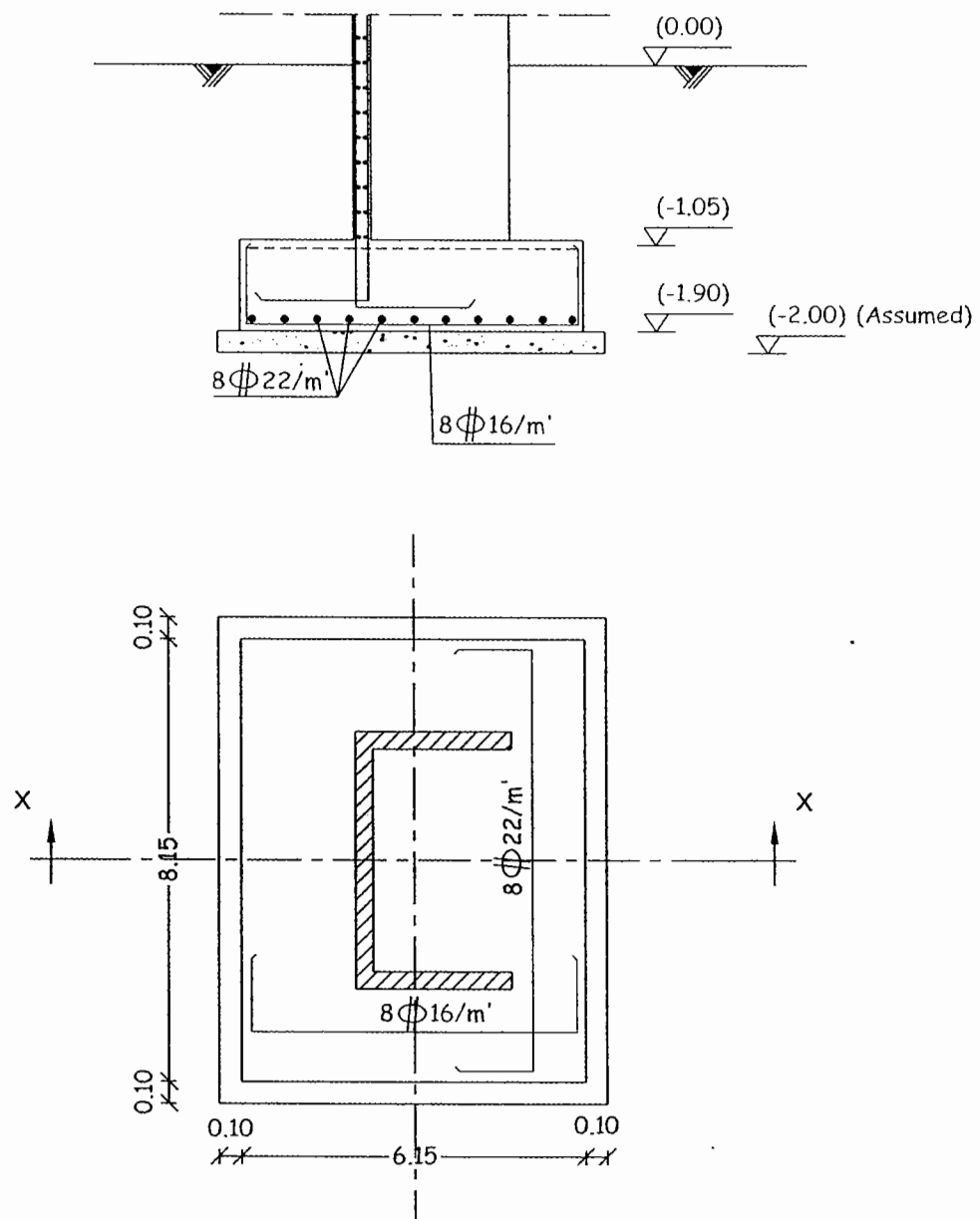
$$A_{s_I} = \frac{M_{u_I} * 10^6}{F_y * J * d} = \frac{371.22 * 10^6}{400 * 0.826 * 780} = 1440 \text{ mm}^2/\text{m}'$$

$$\boxed{8 \phi 16/\text{m}'}$$

$$A_{s_{II}} = \frac{M_{u_{II}} * 10^6}{F_y * J * d} = \frac{695 * 10^6}{400 * 0.826 * 780} = 2696.8 \text{ mm}^2/\text{m}'$$

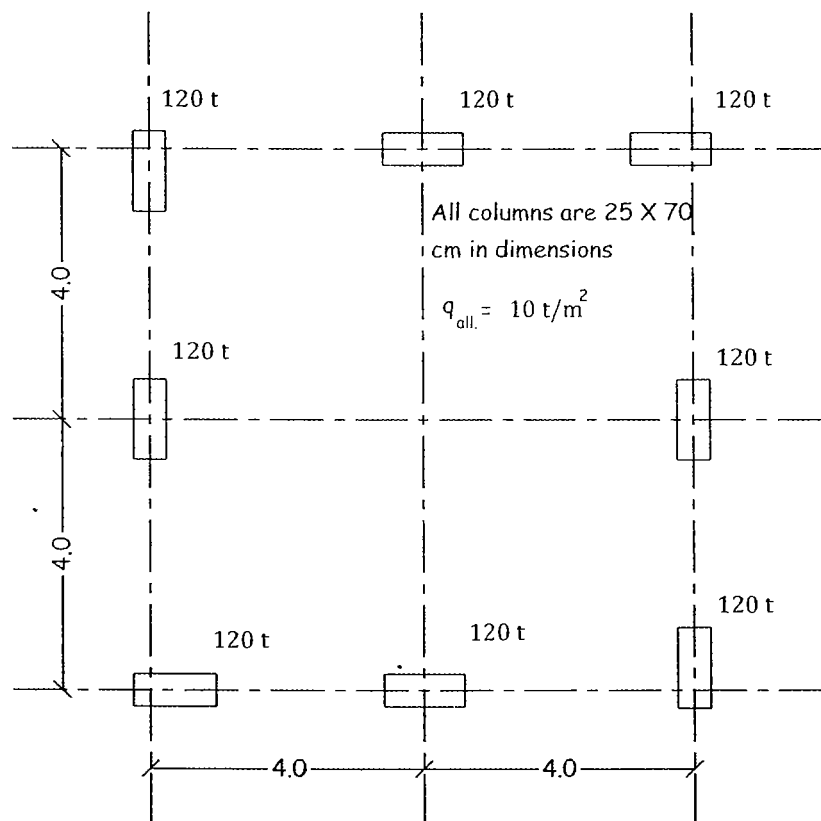
$$\boxed{8 \phi 22/\text{m}'}$$

⑧ Details :-



Example No. (5):-

For the group of columns shown in figure, suggest a suitable type of foundation and calculate the area required in each case. Without design, sketch concrete dimensions and reinforcement details.



Solution:-

- ALL columns are 25 * 70 cm
- $P = 120 \text{ ton} \longrightarrow$ for each column
- $q_{all.} = 10 \text{ t/m}^2$

① Calculate the footing area :-

$$\text{assume } t_{p,c} = 30 \text{ cm} > 20 \text{ cm}$$

$$\therefore A_{p,c} = \frac{120}{10} = 12 \text{ m}^2 = B_{p,c} * L_{p,c} \text{ -----} \rightarrow \textcircled{1}$$

$$L_{p,c} - B_{p,c} = b - a$$

$$L_{p,c} - B_{p,c} = 0.7 - 0.25 = 0.45 \text{ m} \text{ -----} \rightarrow \textcircled{2}$$

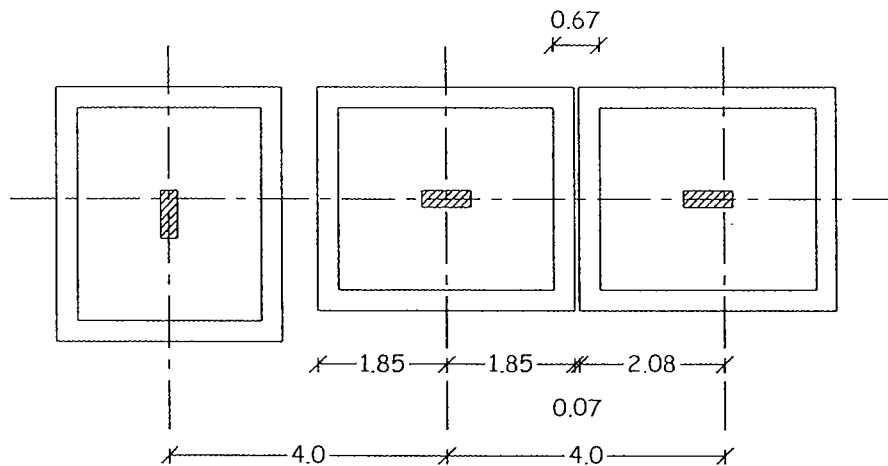
Solving ① & ② :-

$$12 = B_{p,c} * (0.45 + B_{p,c}) \Rightarrow B_{p,c} = 3.24 \approx 3.25 \text{ m}$$

$$L_{p,c} = 0.45 + B_{p,c} = 0.45 + 3.25 = 3.70 \text{ m}$$

$$L_{r,c} = 3.70 - 2 * 0.30 = 3.10 \text{ m}$$

$$B_{r,c} = 3.25 - 2 * 0.30 = 2.65 \text{ m}$$



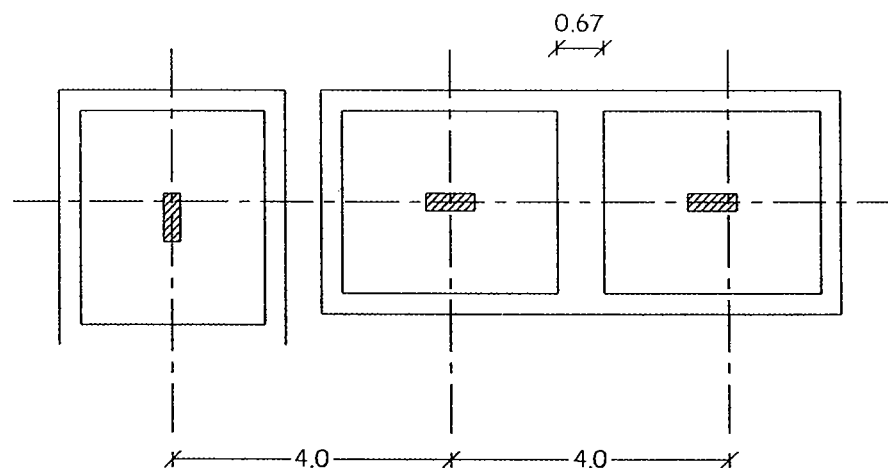
أقل مسافة بين القواعد العادية من الرسم هي 7.0 cm وهى مسافة صغيرة لا يمكننا من

عمل الشدات الخشبية

يمكن دمج القواعد العادية سويا مع ملاحظة ان القواعد المسلحة تبعد عن بعضها البعض

مسافة 67 cm وهى مسافة كافية بين القاعدتين المسلحتين لتوزيع اجهاد كلا منهما على

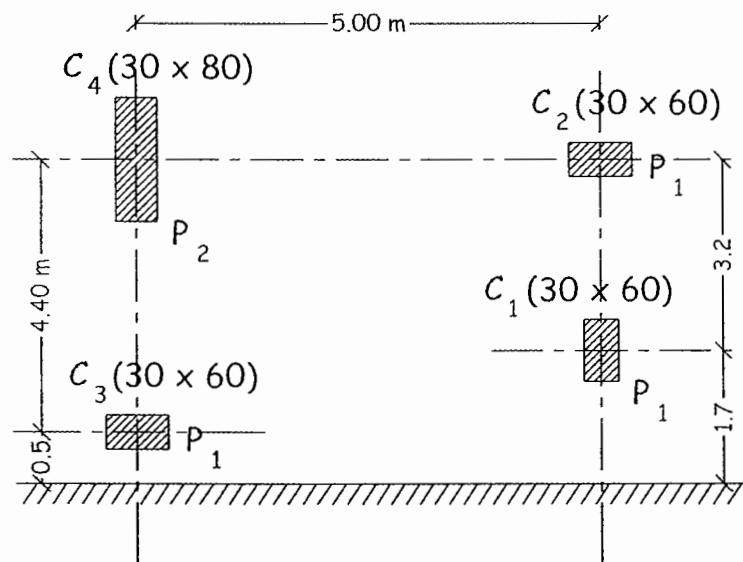
التربية.



Example No. (6):-

For the four columns, shown in the part plan in figure (1), it is required to:

- Suggest the most suitable and economic foundation type for the four columns, and then calculate the required footings concrete horizontal dimensions if the thickness of P.C. is 30 cm, and $q_{all.} = 20 \text{ t/m}^2$.
- Draw a plan with scale 1:50, showing the foundations dimensions.

**Given:-**

$$P_1 = 1000 \text{ KN}$$

$$P_2 = 1300 \text{ KN}$$

Solution:-

- ① C_1 , C_2 , and C_3 have same dimensions and loads, but different geometry.

Try isolated footing

Calculate the footing area :-

$$\therefore t_{P,C} = 30 \text{ cm} > 20 \text{ cm}$$

$$\therefore A_{P,C} = \frac{1000}{200} = 5 \text{ m}^2 = B_{P,C} * L_{P,C} \text{ ----- } \textcircled{1}$$

$$L_{P,C} - B_{P,C} = b - a$$

$$L_{P,C} - B_{P,C} = 0.6 - 0.30 = 0.30 \text{ m} \text{ ----- } \textcircled{2}$$

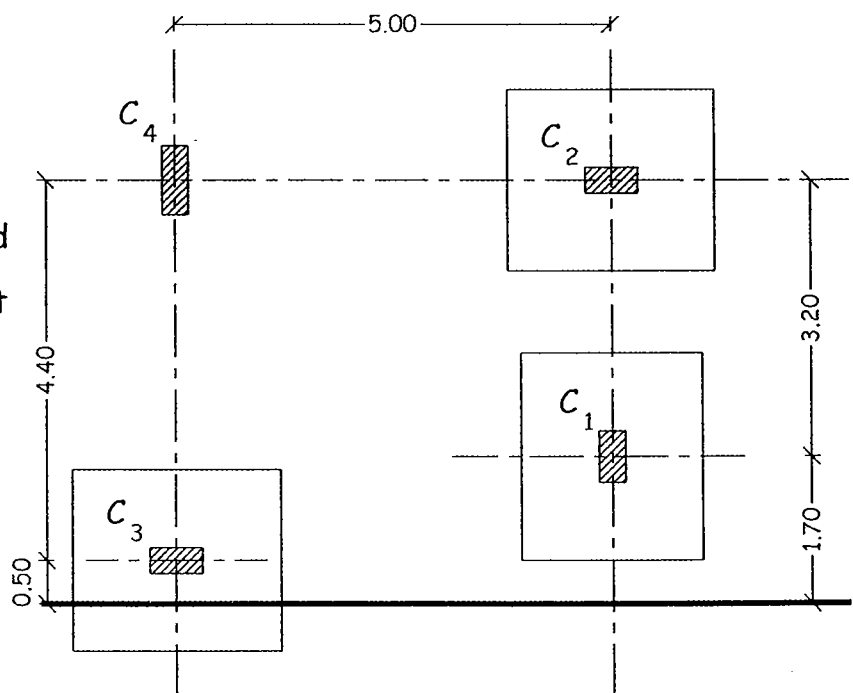
Solving ① & ② :-

$$5 = B_{P,C} * (0.30 + B_{P,C}) \Rightarrow B_{P,C} = 2.09 \approx 2.10 \text{ m}$$

$$L_{P,C} = 0.30 + B_{P,C} = 0.30 + 2.10 = 2.40 \text{ m}$$

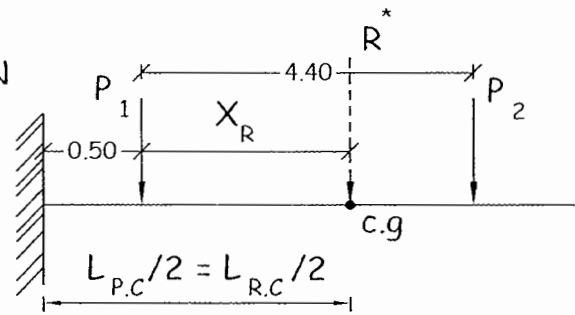
We can use isolated footings for C_1 & C_2 , but not for C_3 .

For C_3 & C_4 , combined rectangular footing, as $S = 4.40 \text{ m}$.



$$R^* = P_1 + P_2 = 1000 + 1300 = 2400 \text{ KN}$$

$$X_R = \frac{1300 * 4.40}{2400} = 2.38 \text{ m}$$



① Calculate the footing area :-

$$\frac{L_{P.C.}}{2} = X_R + D = 2.38 + 0.50 = 2.88 \text{ m} \approx 2.90 \text{ m}$$

$$L_{P.C.} = 2 * 2.90 = 5.80 \text{ m}$$

$$L_{P.C.} = L_{R.C.} = 5.80 \text{ m}$$

$$\therefore t_{P.C.} = 30 \text{ cm} > 20 \text{ cm}$$

$$\therefore A_{P.C.} = \frac{R^*}{q_{all.}} = \frac{2400}{200} = 12 \text{ m}^2 = B_{P.C.} * 5.80$$

$$\therefore B_{P.C.} = \frac{A_{P.C.}}{L_{P.C.}} = \frac{12}{5.80} = 2.06 \text{ m} \approx 2.10 \text{ m}$$

$$B_{R.C.} = 2.10 - 2 * 0.30 = 1.50 \text{ m}$$

②

